## Sartorius <br> YDK 01, YDK 01-0D, YDK 01 LP

Density Determination Kit<br>User's Manual



## YDK 01, YDK 01-OD



## Kit Components

## Die Bestandteile

Contenu de la livraison
1 Beakers (76 mm $\varnothing$ and $55 \mathrm{~mm} \varnothing$ ) Bechergläser
( $\varnothing 76 \mathrm{~mm}$ u. $\varnothing 55 \mathrm{~mm})$
Béchers ( $\varnothing 76 \mathrm{~mm}$ et $\varnothing 55 \mathrm{~mm}$ )
2 Bar frame Gestell
Structure de suspension
3 Thermometer with retainer clip Thermometer mit
Befestigungsklemme Thermomètre avec clip de fixation
4 Glass plummet
Glassenkkörper
Plongeur calibré en verre
5 Sieve for immersing samples
(pan hanger assembly)
Tauchsieb
Panier pour échantillons «flottants» (ensemble à suspendre)
6 Sample holder
(pan hanger assembly)
Tauchkorb
Panier pour échantillons
(ensemble à suspendre)
7 Metal plafform
Brücke
Pont métallique

8 Gasket for ME models Dichtring für ME-Modelle Anneau d'étanchéité pour modèles ME
9 Adapters (3)
Adapter (3 Stück)
Adaptateurs (3)

## YDK 01 LP



## Kit Components <br> Die Bestandteile <br> Contenu de la livraison

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(pan hanger assembly)
Tauchkorb
Panier pour échantillons
(ensemble à suspendre)
7 Metal platform
Brücke
Pont métallique

8 Adapter for LA/LP models with an analytical draft shield Adapter für LA/LP-Waagen mit Analysenwindschutz Adaptateur pour modèles LA/LP avec chambre analytique
9 Adapter for LA/LP models without an analytical draft shield Adapter für LA/LP-Waagen ohne Analysenwindschutz Adaptateur pour modèles LA/LP sans chambre analytique
10 Compensating disk for LA/LP 3200 D models Ausgleichsscheibe für LA/LP 3200 D Disque de compensation pour modèles LA/LP 3200 D

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## With this Sartorius Density Determination Kit

 you have acquired a high-quality accessory to your electronic balance.This accessory kit will ease your daily work load.
Please read the Installation and Operating Instructions carefully before setting up your density determination kit and working with it.
If your balance is equipped with a density determination program, you can have the rho values calculated by the program.
In this case, please follow the operating instructions in "Getting Started."

Perform density determination as described in the density determination program.

## Important Note:

The YDK 01-OD density determination kit can be used for determining the density of liquid according to weights and measures regulations.

## Getting Started <br> YDK 01, YDK 01-OD

You can use the density determination kit, YDK Ol or YDK 01-OD, with the following balances:

- ME series balances (Genius series)
- BA balances with a readability $\leq 0.1 \mathrm{mg}$
- BP/LA balances with a readability $\leq 0.1 \mathrm{mg}$
- MC balances with a weighing range of 210 g and up (Micro series)
- RC balances (Research series)


## Preparing the Bar Frame

You must mount the adapter before the bar frame can be placed on the balance.
Please use the adapter that is appropriate for the balance you are using.
(approx. dimensions)

$8 \mathrm{~mm} \varnothing$, height $41.3 \mathrm{~mm}-$ ME balance
with gasket

| 8 | $7 \mathrm{~mm} \varnothing$, height 16.5 mm | - BA, BP*, MC and RC balances |
| :---: | :---: | :---: |
| $\square$ | $12 \mathrm{~mm} \varnothing$, height 25.5 mm | - BP**/LA balances with a readability $\leq 0.1 \mathrm{mg}$ |

$$
\begin{aligned}
*= & B P 210 \text { D, BP } 300 \mathrm{~S}, \mathrm{BP} 210 \mathrm{~S}, \mathrm{BP} 160 \mathrm{P}, \\
& \text { BP } 110 \mathrm{~S} \\
* *= & \text { BP } 211 \mathrm{D}, \mathrm{BP} 301 \mathrm{~S}, \mathrm{BP} 221 \mathrm{~S}, \mathrm{BP} 161 \mathrm{P}, \\
& \text { BP } 121 \mathrm{~S}
\end{aligned}
$$



Screw the appropriate adapter into the underside of the bar frame base.


Now remove the following components from the balance:

- weighing pan
- compensating ring for BA and BP balances - pan support for BA and BP balances

Place the frame in the weighing chamber. The wedge-shaped opening at the top of the frame must face the direction from which the sample holder (sieve/glass plummet) will be placed into the frame.
Always use the metal plafform to hold a beaker. Please position this plafform through the frame so it rests evenly on the base of the weighing chamber. If you are using an $\mathrm{BA}, \mathrm{BP}$ or ME balance, turn the plafform so it rests on the pins which are far apart. For $R C$ and MC balances, the plafform should rest on the pins which are closer together.

## YDK 01 LP



## LA/LP Balances, Except Model LA/LP3200D

- Place the components on the balance in the following order:
- Compensating ring
- Bar frame

O The wedge-shaped opening at the top of the bar frame should face the direction from which the sample holder (pan hanger assembly/glass plummet) will be placed on the balance

## LA3200D, LP3200D Balances

- Place the components on the balance in the following order:
- Short adapter
- Compensating disk
- Bar frame

O The wedge-shaped opening at the top of the bar frame should face the direction from which the sample holder (pan hanger assembly/glass plummet) will be placed on the balance


LA/LP Balances, Except Model LA/LP3200D with the YDSO1LP Draft Shield

- Place the components on the balance in the following order:
- Longer adapter
- Bar frame

O The wedge-shaped opening at the top of the bar frame should face the direction from which the sample holder (pan hanger assembly/glass plummet) will be placed on the balance


## LA3200D, LP3200D Balances with the YDS01LP Draft Shield

- Place the components on the balance in the following order:
- Longer adapter
- Compensating ring
- Bar frame

O The wedge-shaped opening at the top of the bar frame should face the direction from which the sample holder (pan hanger assembly/glass plummet) will be placed on the balance

## Beaker/Immersion Device



- Use the metal plate to support the beaker.

Place it on the bar frame base and then set both on the balance.

The choice of the beaker and the immersion device depends on the sample to be determined (see below).


To determine the specific gravity of solids when their density is greater than that of the liquid in which the sample is immersed, use:

- $76 \mathrm{~mm} \varnothing$ beaker and sample holder


To determine the specific gravity of solids when their density is less than that of the liquid in which the sample is immersed, use:

- $76 \mathrm{~mm} \varnothing$ beaker and sieve for immersing the sample


To determine the density of liquids:

- $55 \mathrm{~mm} \varnothing$ beaker and glass plummet


## Thermometer

If necessary, attach the thermometer to the rim of the beaker using the retainer clip.

## Methods for Determining Specific Gravity/Density

The Archimedean principle is applied for determining the specific gravity of a solid with this measuring device:
A solid immersed in a liquid is exposed to the force of buoyancy. The value of this force is the same as that of the weight of the liquid displaced by the volume of the solid.

With a hydrostatic balance which enables you to weigh a solid in air as well as in water, it is possible to:
determine the specific gravity of a solid if the density of the liquid causing buoyancy is known:
$\rho=\frac{W(a) \cdot \rho(f l)}{W(a)-W(f)}$
or
determine the density of a liquid if the volume of the immersed solid is known:
$\rho(f)=\frac{G}{V}$
where:
$\rho \quad=$ specific gravity of the solid
$\rho(f)=$ density of the liquid
W $(\mathrm{a})=$ weight of the solid in air
$W(f)$ = weight of the solid in liquid
G = buoyancy of the immersed solid
$\vee \quad=$ volume of the solid

## Sources of Error and Possibilities for Correction

The formula on the previous page for determining the specific gravity of solids is sufficient to obtain an accuracy of one to two decimal places.
Depending on the accuracy you require, consider the following error and allowance factors.

- The density of the liquid causing buoyancy depends on its temperature
- Air buoyancy during weighing in air
- The change in the immersion level of the pan hanger assembly when the sample is immersed
- Adhesion of the liquid on the suspension wire of the pan hanger assembly
- Air bubbles on the sample

Some of these errors can be corrected by calculation. To do so, it is necessary to proceed as follows:

- measure the temperature of the reference liquid and correct its density accordingly
and
- define the inner diameter of the container which holds the reference liquid.


## Dependence of the Liquid Density on Temperature

The density of the liquid causing buoyancy depends on the temperature. The change in the density per ${ }^{\circ} \mathrm{C}$ change in temperature is in the range of - 0.02\% for distilled water

- $0.1 \%$ for alcohols and hydrocarbons.

In other words, this can show up in the third decimal place during specific gravity/density determination.

To correct the liquid density for temperature, proceed as follows:

- measure the temperature of the liquid using the thermometer that comes with the kit
- use the table at the back of this manual to find the density of the most commonly used liquids, water and ethanol, at the temperature measured, and use this density for the value $\rho(f)$.


## Air Buoyancy

A volume of 1 cm of air has a weight of approximately 1.2 mg , depending on its temperature, humidity and air pressure. When weighed in air, a solid is buoyed by a corresponding force per $\mathrm{cm}^{3}$ of its volume. The error that results if the air buoyancy is not allowed for shows up in the third decimal place and should therefore be corrected.
The following formula allows for air buoyancy:
$\rho=\frac{W(a) \cdot[\rho(f)-\rho(a)]}{W(a)-W(f)}+\rho(a)$.
Where $\rho(\mathrm{a})=0.0012 \mathrm{~g} / \mathrm{cm}^{3}=$ Density of air under standard conditions (temperature $20^{\circ} \mathrm{C}$, pressure 101.325 kPa ).

## Depth of Immersion

The pan for holding and/or immersing the sample during weighing in liquid is rigidly attached to two wires and is immersed approximately 30 mm below the surface of the liquid. Since the balance is tared before each measurement, the addifional buoyancy caused by the immersed part of the measuring device is not allowed for in the specific gravity determination.
When a solid sample is weighed in liquid, a volume of the liquid will be displaced which corresponds to the volume of the solid sample. This causes the attachment wires of the pan hanger assembly to be immersed deeper and generate additional buoyancy which introduces an error in the specific gravity determination.

Use the following formula to correct this error:
$\rho=\frac{W(a) \cdot[\rho(f)-\rho(a)]}{0.99983[W(a)-W(f)]}+\rho(a)$
Since the correction factor is determined exclusively by the geometry of the measuring device setup, be sure to only use the large diameter beaker ( 76 mm ) from the kit when determining the specific gravity of a solid. The "Supplement" to this manual shows how this correction factor is derived.

## Adhesion of Liquid to the Wire

When the sample holder (or sieve) is immersed in liquid causing buoyancy, liquid travels up the wire because of adhesion forces and generates an additional weight in the range of a few milligrams.
Since the sample holder (or sieve) is in the liquid causing buoyancy during both weighing in air and weighing in liquid, and the balance is tared at the beginning of each measuring procedure, the effect of the meniscus can be disregarded.
To reduce the surface tension and the friction of liquid on the wire, add three drops of a tenside (Mirasol Antistatic or an ordinary dishwashing detergent) to the distilled water in the beaker.

Because of the liquid travelling up the wire, the weight may slowly change even after the stability symbol " $g$ " appears. Therefore, read off the weight immediately after the " $g$ " is displayed.

## Air Bubbles

The measuring error caused by air bubbles adhering to the sample can be estimated in the following manner. An air bubble with a diameter of 0.5 mm causes an additional buoyancy of less than 0.1 mg when a sample is weighed in water. An air bubble diameter of 1 mm causes additional buoyancy of 0.5 mg and an air bubble diameter of 2 mm causes approx. 4.2 mg additional buoyancy. Larger air bubbles must be removed with a fine brush or other utensil.
You can also wet the sample in a separate container before you weigh it.

## Determining the Specific Gravity/Density

## Determining the Specific Gravity of Solids

## Preparation

(Distilled water is used in the description)

- Center the large-diameter beaker ( $76 \mathrm{~mm} \varnothing$ ) on the metal plafform
- Fill it so that the distilled water is approximately 5 mm below the rim
- Add three drops of tenside to the distilled water
- Attach the thermometer to the rim of the beaker using the retainer clip
- Clean the sample holder with a solvent lespecially the wires that will be immersed) and hang it from the frame


## Measuring Procedure

## Determining the Weight of a Sample in Air

- Tare the balance
- Place the sample on the upper pan on the frame and weigh
- Record the weight W (a)

Determining the Buoyancy $G=W(a)-W(f)$

- Tare the balance with the sample on the upper pan on the frame
- Place the sample in the sample holder')
- Record the absolute readout of the buoyancy " $G$," which is displayed with a negative sign
${ }^{1}$ I If you remove the pan hanger assembly from the measuring device to do this, make sure that no additional air bubbles are on it when you re-immerse it; it is better to place the sample directly on the pan using forceps or a similar utensil.


## Calculating the Specific Gravity

- Read off the temperature of the liquid
- Using the tables at the back of this manual, find the density $\rho(f)$ which corresponds to the temperature measured for the liquid you are using
- Calculate specific gravity using the following formula:
$\rho=\frac{W(a) \cdot\left[\rho(f)-0.0012 \mathrm{~g} / \mathrm{cm}^{3}\right]}{0.99983 \mathrm{G}}+0.0012 \mathrm{~g} / \mathrm{cm}^{3}$
$W(\mathrm{a})$ and G in $\mathrm{g} ; \rho(\mathrm{fl})$ in $\mathrm{g} / \mathrm{cm}^{3}$
$G=W(a)-W(f)$


## Determining the Specific Gravity of Solids with a Density Less Than $1 \mathrm{~g} / \mathrm{cm}^{3}$

There are two different methods for determining the specific gravity of solids with a density less than $1 \mathrm{~g} / \mathrm{cm}$.

## Method 1:

For this method, distilled water is still used as the liquid causing buoyancy, but the pan hanger assembly is replaced by the sieve for immersing samples.
To determine the sample's buoyancy, float it on the surface of the water and then immerse it using the sieve.
It is also possible to use forceps or a similar tool to place the sample directly under the sieve (without removing the sieve from the frame).
If the buoyancy of the substance to be measured is so high that the weight of the sieve is not enough to immerse the sample, increase the weight of the sieve by adding an additional weight to the upper pan on the frame.

## Method 2:

(for this method, use the sample holder)
Here, use a liquid for causing buoyancy with lower density than that of the solid for which the specific gravity is to be determined. We have had good results with ethanol (up to a density of approx. $0.8 \mathrm{~g} / \mathrm{cm}^{3}$ ).
The density $\rho$ (fl) of ethanol (with regard to its temperature) can be found in the table in the supplement.
The negative effect of the liquid's surface tension on the results is less noticeable when ethanol is used than when distilled water is employed. Therefore, it is not necessary to add tensides.
When working with ethanol, you must observe the valid safety precautions.
Use method 2 if the density of the solid varies only slightly from that of distilled water. Since the sample is suspended in water, measuring errors may occur if the first method is used.
It also makes sense to use the second method when determining the specific gravity of a granulated substance, since it would be difficult to get the entire sample under the sieve as required when performing the first method.
Do not use ethanol if the sample could be attacked or dissolved by it.

## Preparation (for Method 1 only)

(Distilled water is used in the description.)

- Center the large-diameter beaker ( $76 \mathrm{~mm} \varnothing$ ) on the metal plafform
- Fill it so that the distilled water is approximately 5 mm below the rim
- Add three drops of tenside to the distilled water
- Attach the thermometer to the rim of the beaker using the retainer clip
- Clean the sieve with a solvent (especially the wires that will be immersed) and hang it from the frame


## Measuring Procedure (for Method 1 only)

## Determining the Weight of the Sample in Air

- Tare the balance
- Place the sample on the frame weighing pan and weigh
- Record the weight W (a)


## Determining the Buoyancy $G=W(a)-W(f)$

- Tare the balance again (with the sample on the frame weighing pan)
- Place the sample under the sieve or immerse it below the surface of the liquid using the sieve')
- Record the buoyancy " $G$," which is displayed with a negative sign


## Calculating the Specific Gravity

- Read off the temperature of the liquid
- Using the table at the back of this manual, find the density $\rho(f)$ which corresponds to the temperature measured for distilled water
- Calculate the specific gravity using the following formula:
$\rho=\frac{W(a) \cdot \rho(f)}{0.99983 G}+0.0012 \mathrm{~g} / \mathrm{cm}^{3}$
W (a) and G in g; $\rho(f)$ in $\mathrm{g} / \mathrm{cm}^{3}$
$G=W(a)-W(f)$
${ }^{1}$ I If you remove the pan hanger assembly from the measuring device to do this, make sure that no additional air bubbles are on it when you re-immerse it in the liquid; it is better to place the sample directly under the pan using forceps, etc.


## Determining the Density of Liquids

## Preparation

- Center the small-diameter beaker ( $55 \mathrm{~mm} \varnothing$ ) on the metal platform
- Attach the thermometer to the rim of the beaker using the retainer clip


## Measuring Procedure

- Suspend the disk with the glass plummet (hanging on one wire) from the frame
- Tare the balance
- Fill the beaker with the liquid to be determined so that the liquid is 10 mm above the glass plummet


## Determining the Buoyancy $G=W(a)-W(f)$

The negative weight displayed by the balance corresponds to the buoyancy acting on the glass plummet in the liquid.

- Record the buoyancy displayed with a negative sign
- Read off the temperature and record it also


## Calculating the Density

- Calculate the density using the following formula:
$\rho(f)=\frac{G}{V}$
Ging; $V$ in $\mathrm{cm}^{3}$
The glass plummet included in the specific gravity/density determination kit has a volume of $10 \mathrm{~cm}^{3}$.

It is easy to obtain the current density of the liquid (in $\mathrm{g} / \mathrm{cm}^{3}$ ); you will not need a calculator. Mentally shift the decimal point in the balance display one place to the left.

## Application in Legal Metrology

The density determination kit, YDK O1-OD, may only be used in legal metrology to determine the density of liquids.
In addition to the bar frame, adapter and metal plate, the following components provided with the YDK O1-OD will be needed:

- Beaker
- Glass plummet
- Verified thermometer: Designed in accordance with EO 14.1

Scale of $15-25^{\circ} \mathrm{C}$
Readability, $0.1^{\circ} \mathrm{C}$
Accuracy, $\pm 0.1^{\circ} \mathrm{C}$

## Tables

Density of $\mathrm{H}_{2} \mathrm{O}$ at Temperature T (in ${ }^{\circ} \mathrm{C}$ )

| $\mathrm{T} /{ }^{\circ} \mathrm{C}$ | 0.0 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10. | 0.99973 | 0.99972 | 0.99971 | 0.99970 | 0.99969 | 0.99968 | 0.99967 | 0.99966 | 0.99965 | 0.99964 |
| 11. | 0.99963 | 0.99962 | 0.99961 | 0.99960 | 0.99959 | 0.99958 | 0.99957 | 0.99956 | 0.99955 | 0.99954 |
| 12. | 0.99953 | 0.99951 | 0.99950 | 0.99949 | 0.99948 | 0.99947 | 0.99946 | 0.99944 | 0.99943 | 0.99942 |
| 13. | 0.99941 | 0.99939 | 0.99938 | 0.99937 | 0.99935 | 0.99934 | 0.99933 | 0.99931 | 0.99930 | 0.99929 |
| 14. | 0.99927 | 0.99926 | 0.99924 | 0.99923 | 0.99922 | 0.99920 | 0.99919 | 0.99917 | 0.99916 | 0.99914 |
| 15. | 0.99913 | 0.99911 | 0.99910 | 0.99908 | 0.99907 | 0.99905 | 0.99904 | 0.99902 | 0.99900 | 0.99899 |
| 16. | 0.99897 | 0.99896 | 0.99894 | 0.99892 | 0.99891 | 0.99889 | 0.99887 | 0.99885 | 0.99884 | 0.99882 |
| 17. | 0.99880 | 0.99879 | 0.99877 | 0.99875 | 0.99873 | 0.99871 | 0.99870 | 0.99868 | 0.99866 | 0.99864 |
| 18. | 0.99862 | 0.99860 | 0.99859 | 0.99857 | 0.99855 | 0.99853 | 0.99851 | 0.99849 | 0.99847 | 0.99845 |
| 19. | 0.99843 | 0.99841 | 0.99839 | 0.99837 | 0.99835 | 0.99833 | 0.99831 | 0.99829 | 0.99827 | 0.99825 |
| 20. | 0.99823 | 0.99821 | 0.99819 | 0.99817 | 0.99815 | 0.99813 | 0.99811 | 0.99808 | 0.99806 | 0.99804 |
| 21. | 0.99802 | 0.99800 | 0.99798 | 0.99795 | 0.99793 | 0.99791 | 0.99789 | 0.99786 | 0.99784 | 0.99782 |
| 22. | 0.99780 | 0.99777 | 0.99775 | 0.99773 | 0.99771 | 0.99768 | 0.99766 | 0.99764 | 0.99761 | 0.99759 |
| 23. | 0.99756 | 0.99754 | 0.99752 | 0.99749 | 0.99747 | 0.99744 | 0.99742 | 0.99740 | 0.99737 | 0.99735 |
| 24. | 0.99732 | 0.99730 | 0.99727 | 0.99725 | 0.99722 | 0.99720 | 0.99717 | 0.99715 | 0.99712 | 0.99710 |
| 25. | 0.99707 | 0.99704 | 0.99702 | 0.99699 | 0.99697 | 0.99694 | 0.99691 | 0.99689 | 0.99686 | 0.99684 |
| 26. | 0.99681 | 0.99678 | 0.99676 | 0.99673 | 0.99670 | 0.99668 | 0.99665 | 0.99662 | 0.99659 | 0.99657 |
| 27. | 0.99654 | 0.99651 | 0.99648 | 0.99646 | 0.99643 | 0.99640 | 0.99637 | 0.99634 | 0.99632 | 0.99629 |
| 28. | 0.99626 | 0.99623 | 0.99620 | 0.99617 | 0.99614 | 0.99612 | 0.99609 | 0.99606 | 0.99603 | 0.99600 |
| 29. | 0.99597 | 0.99594 | 0.99591 | 0.99588 | 0.99585 | 0.99582 | 0.99579 | 0.99576 | 0.99573 | 0.99570 |
| 30. | 0.99567 | 0.99564 | 0.99561 | 0.99558 | 0.99555 | 0.99552 | 0.99549 | 0.99546 | 0.99543 | 0.99540 |

Density of Ethanol at Temperature T (in ${ }^{\circ} \mathrm{C}$ )

| $\mathrm{T} /{ }^{\circ} \mathrm{C}$ | 0.0 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10. | 0.79784 | 0.79775 | 0.79767 | 0.79758 | 0.79750 | 0.79741 | 0.79733 | 0.79725 | 0.79716 | 0.79708 |
| 11. | 0.79699 | 0.79691 | 0.79682 | 0.79674 | 0.79665 | 0.79657 | 0.79648 | 0.79640 | 0.79631 | 0.79623 |
| 12. | 0.79614 | 0.79606 | 0.79598 | 0.79589 | 0.79581 | 0.79572 | 0.79564 | 0.79555 | 0.79547 | 0.79538 |
| 13. | 0.79530 | 0.79521 | 0.79513 | 0.79504 | 0.79496 | 0.79487 | 0.79479 | 0.79470 | 0.79462 | 0.79453 |
| 14. | 0.79445 | 0.79436 | 0.79428 | 0.79419 | 0.79411 | 0.79402 | 0.79394 | 0.79385 | 0.79377 | 0.79368 |
| 15. | 0.79360 | 0.79352 | 0.79343 | 0.79335 | 0.79326 | 0.79318 | 0.79309 | 0.79301 | 0.79292 | 0.79284 |
| 16. | 0.79275 | 0.79267 | 0.79258 | 0.79250 | 0.79241 | 0.79232 | 0.79224 | 0.79215 | 0.79207 | 0.79198 |
| 17. | 0.79190 | 0.79181 | 0.79173 | 0.79164 | 0.79156 | 0.79147 | 0.79139 | 0.79130 | 0.79122 | 0.79113 |
| 18. | 0.79105 | 0.79096 | 0.79088 | 0.79079 | 0.79071 | 0.79062 | 0.79054 | 0.79045 | 0.79037 | 0.79028 |
| 19. | 0.79020 | 0.79011 | 0.79002 | 0.78994 | 0.78985 | 0.78977 | 0.78968 | 0.78960 | 0.78951 | 0.78943 |
| 20. | 0.78934 | 0.78926 | 0.78917 | 0.78909 | 0.78900 | 0.78892 | 0.78883 | 0.78874 | 0.78866 | 0.78857 |
| 21. | 0.78849 | 0.78840 | 0.78832 | 0.78823 | 0.78815 | 0.78806 | 0.78797 | 0.78789 | 0.78780 | 0.78772 |
| 22. | 0.78763 | 0.78755 | 0.78746 | 0.78738 | 0.78729 | 0.78720 | 0.78712 | 0.78703 | 0.78695 | 0.78686 |
| 23. | 0.78678 | 0.78669 | 0.78660 | 0.78652 | 0.78643 | 0.78635 | 0.78626 | 0.78618 | 0.78609 | 0.78600 |
| 24. | 0.78592 | 0.78583 | 0.78575 | 0.78566 | 0.78558 | 0.78549 | 0.78540 | 0.78532 | 0.78523 | 0.78515 |
| 25. | 0.78506 | 0.78497 | 0.78489 | 0.78480 | 0.78472 | 0.78463 | 0.78454 | 0.78446 | 0.78437 | 0.78429 |
| 26. | 0.78420 | 0.78411 | 0.78403 | 0.78394 | 0.78386 | 0.78377 | 0.78368 | 0.78360 | 0.78351 | 0.78343 |
| 27. | 0.78334 | 0.78325 | 0.78317 | 0.78308 | 0.78299 | 0.78291 | 0.78282 | 0.78274 | 0.78265 | 0.78256 |
| 28. | 0.78248 | 0.78239 | 0.78230 | 0.78222 | 0.78213 | 0.78205 | 0.78196 | 0.78187 | 0.78179 | 0.78170 |
| 29. | 0.78161 | 0.78153 | 0.78144 | 0.78136 | 0.78127 | 0.78118 | 0.78110 | 0.78101 | 0.78092 | 0.78084 |
| 30. | 0.78075 | 0.78066 | 0.78058 | 0.78049 | 0.78040 | 0.78032 | 0.78023 | 0.78014 | 0.78006 | 0.77997 |

## Supplement

This supplement should help you to better understand how the formulas and allowance factors used have been derived.

## Fundamental Principles

Density $=\frac{\text { Mass (g) }}{\text { Volume }\left(\mathrm{cm}^{3}\right)}$
The Archimedean Principle:
A solid immersed in a liquid is exposed to the force of buoyancy (G). This value is the same as that of the weight of the liquid displaced by the volume of the solid.
The volume of an immersed solid $V(s)$ equals the volume of the displaced liquid $V(f)$ ).
The following are determined:

1. The weight of the sample in air: $W$ (a)
2. The buoyancy of the solid in liquid: $G$

The specific gravity of a solid is:
$\rho=\frac{\text { sample mass }}{\text { sample volume }}=\frac{W(a)}{V(s)}=\frac{W(a)}{V(f)}$
If the density $\rho(f)$ ) of the displaced liquid is known, then
$V(f)=\frac{\operatorname{Mass}(f l)}{\rho(f))}=\frac{G}{\rho(f)}$
Therefore:
$\rho=\frac{W(a) \cdot \rho(f f)}{G}$

## Calculation

The specific gravity of a solid is calculated from the ratio
$\rho: W(a)=\rho(f): W(a)-W(f)$,
where:
$\rho=\frac{W(a) \cdot \rho(f f)}{W(a)-W(f l)}$
$W(a)-W(f f)=G=$ buoyancy of the sample

The density of a liquid is determined from the buoyancy of the plummet, which has a defined volume
$\rho(f)=\frac{G}{V}$
where:
$\rho \quad=$ specific gravity of a solid
$\rho(f)$ ) density of the liquid
$W(a)=$ weight of the solid in air
$W(f)$ = weight of the solid in liquid
G = buoyancy of the plummet
$\vee \quad=$ volume of the solid

## Allowance Factors

You must allow for the following when determining the specific gravity of solids:

- the air buoyancy that affects the sample weighed in air
where $\rho(\mathrm{a})=0.0012 \mathrm{~g} / \mathrm{cm}^{3}=$ density of air under standard conditions
(temperature $20^{\circ} \mathrm{C}$, pressure 101.325 kPa );
which results in the following:
$\rho=\frac{W(a) \cdot[\rho(f)-\rho(a)]}{W(a)-W(f)}+\rho(a)$
- the immersion of the wires of the sample holder or sieve

When using this specific gravity determination kit, you must multiply the buoyancy $G=[W(a)-W(f)]$ by the factor 0.99983 (Corr).
Therefore:
$\rho=\frac{W(a) \cdot[\rho(f)-\rho(a)]}{[W(a)-W(f)] \cdot \text { Korr }}+\rho(a)$
This factor allows for the buoyancy of the wires which are submerged deeper when the sample is in the sample holder.

## How this allowance factor is derived:

The buoyancy caused by the submerged wires depends on the height " $h$ " by which the liquid rises when the sample is immersed.

Here, the sample volume V (pr) corresponds to the liquid volume $\mathrm{V}(\mathrm{ff})$. The sample volume is determined by measuring the buoyancy. Hence, it is:
$\mathrm{V}(\mathrm{pr})=\mathrm{V}(\mathrm{fl})$
or
$\frac{W(a)-W(f))}{\rho(f l)}=\frac{\pi \cdot h \cdot D^{2}}{4}$
Therefore, $h=\frac{4 \cdot[W(a)-W(f)]}{\rho(f) \cdot \pi \cdot D^{2}}$
The buoyancy " $A$ " caused by the immersed wires is:
$A=2 \cdot \frac{\pi-d^{2}}{4} \cdot h \cdot \rho(f)$
When " $h$ " is used:
$A=\frac{\left.2 \cdot \pi \cdot d^{2} \cdot 4 \cdot[W(a)-W(f)] \cdot \rho(f)\right)}{4 \cdot \rho(f) \cdot \pi \cdot D^{2}}$
$A=2 \cdot \frac{d^{2}}{D^{2}} \cdot[W(a)-W(f)]$
To allow for the buoyancy of the wires, subtract the buoyancy " A " caused by the immersed wires from the buoyancy determined for the sample: $G=W(a)-W(f)$. The corrected buoyancy "A (corr)" to use in this calculation is then: G-"A."
$A($ corr $)=[W(a)-W(f)]-2 \cdot \frac{d^{2}}{D^{2}} \cdot[W(a)-W(f)]$
$A($ corr $)=\left[1-2 \cdot \frac{d^{2}}{D^{2}}\right] \cdot[W(a)-W(f)]$
The specific gravity determination kit uses the large-volume beaker ( $76 \mathrm{~mm} \varnothing$ ) and an immersing device with 2 wires ( 0.7 mm diameter) for the determination of the specific gravity of solids.
When the values $d=0.7 \mathrm{~mm}$ and $\mathrm{D}=76 \mathrm{~mm}$ are plugged in the equation, the correction factor is:
$1-2 \cdot \frac{0.7^{2}}{76^{2}}=0.99983$
When using devices with other dimensions, the correction factor must be recalculated.

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